

# Agent-based agreement over concept meaning using contrast sets

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**Abstract.** We develop a model for 2 agents to reach agreement over concept meaning in specific contexts. The model is based on an argumentation-based communication that engage the agents in a process of mutual adaptation using argumentation to reach an agreement over concept meaning. Our approach is to model concept meaning using the semiotic triangle and the notion of contrast sets. We implement and evaluate present three common sense scenarios where two agents argue and reach agreements over the contextual meaning of concepts.

**Keywords.** Multiagent systems, shared semantics, agreement technologies

## Introduction

Languages are a way to exchange information. However, those languages are used in a particular perspective and follows particular rules that determines the meaning of linguistic signs. If either the perspective or the rules are not completely shared by two speakers it can lead to a disagreement over the meaning.

Our long term research goal is to develop a computational model of contextual meaning agreement in a multiagent system (MAS) setting. Our assumption is not only than meaning is context-dependent, but an agreement on meaning is often negotiated among participating agents in a specific context. The approach we take is that two agents, using argumentation-based communication, can detect misunderstandings (disagreements), and engage in a process of mutual adaptation, also using argumentation, to reach an agreement over meaning (with respect of the concepts used in some context). In order to do so, we implemented agents with contrast sets. A contrast set contains different segregates of the environment [2], each of them linked to a particular sign. Each contrast set is associated to a particular social context. To model the process of argumentation, we choose to represent our signs as a part of a semiotic triangle [5] along with an intensional and an extensional definition. Using the semiotic triangle with the argumentation theory [3] we show that it is possible to solve disagreements in several basic scenarios, including synonyms and hyponyms, by creating new contrast sets.

The structure of this paper is as follows: we start by presenting the motivation of our goals and the main background notions we use (semiotic triangle and contrast set), then Section 2 presents our approach to reach those goals in a set of limited scenarios, that are later explained in Section 3, where we also explain the results of a prototype implementation. The closes with a discussion on the current approach and future work on more generic scenario.

## 1. Motivation

Our approach to model contextual meaning is based on the notion of *contrast set* developed in ethnographic studies of how people actually use (give meaning to) words [2]. A contrast set is a collection of segregates, and a *segregate* is a “terminologically distinguished array of objects”. For instance, a buyer can enter an eatery and ask “What kind of sandwiches ya got besides hamburgers and hot dogs?”, to which the seller responds “How about a ham ’n cheese sandwich?”. Here the collection of words describing the different kinds of products one can eat are the contrasts set: hamburgers, hot dog, ham ’n cheese sandwich, etc. However, the way one person segregates and the word or sign used to reference them is contextual, which can lead to misunderstandings that will require, to be resolved, some adaptation of the intended meaning. An example of misunderstanding (from [2]) is the client complaining with a sentence like this: “Hey, that’s no hamburger; that’s a cheeseburger!”. The origin of the misunderstanding is that the client is considering *hamburger* and *cheeseburger* as two different in the contrast set he is using to conceptualize the eating options, while the common (or default) meaning of cheeseburger is that it is a *kind of hamburger*.

The “meaning as usage” paradigm comes from Wittgenstein’s *Philosophical Investigations*, and is the underpinning of ethnographic notions like a contrast set in a particular context or language game. We will approach this large problem in a limited way, in scenarios where agents can negotiate an agree on meaning by building new contrast sets in a new context.

As a running example of context-dependent meaning we will use the common sense domain of *Furniture Shopping*. Let’s assume they have some default meaning of some concepts (often called Ontologies in Artificial Intelligence), for instance about furniture. If we ask the agents before they interact if an armchair is a chair they would probably answer affirmatively. For our purposes, we can set that armchair is a sub-concept of the chair concept. Now, imagine the buyer enters the shop and tells the seller this: “I wan to buy one armchair and four chairs”. If the seller understands the meaning intended by the buyer no misunderstanding arises, and the will keep talking about “chairs” and referring to particular objects in the shop that are “chairs” without any disagreement on any specific object. And, nevertheless, they are not using “chair” as the same concept as before: now the concept chair in fact means “chairs without arms”. This so because the buyer has created the contrast set  $\{armchair, chair\}$ , and by doing so he has (implicitly) decided to use the word “chair” with a new intended meaning. If the two agents consistently use the term “chair” to refer only to objects in the shop that are chairs and are not armchairs, we say they have achieved an agreement

on meaning. This “shift” in the meaning of a term or word is so pervasive that we humans are hardly aware of it, but we would consider very wrong if the seller tried to sell three armchairs and two chairs without arms (which is consistent with the default meaning of chair and armchair).

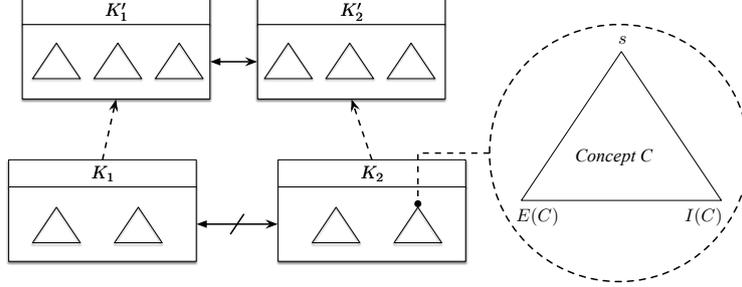
Now, the issue we need to address is how to represent concept meaning in a way that allows us to have a computational model in which this “shift” in the meaning by creating contrast sets. The approach is semiotic, in which a *concept* is represented by a semiotic triangle  $\langle S, I, E \rangle$  with three components: a sign  $S$ , a meaning (or *intensional definition*), and an object or reference (or *extensional definition*) [5]. In this view, a sign like “chair” can have two different meanings in the *Furniture shopping* scenario by being in two different semantic triangles. What we called the default meaning is that often found in dictionaries and ontologies, that specifies the typical or more frequent sense of a sign like “chair”, and could be expressed in a semiotic triangle  $\langle \text{“chair”}, I, E \rangle$  where  $I$  is the default meaning of chairs (including armchairs and other sorts of chairs), and  $E$  is the objects that can be referred to by that sign. However, after the buyer introduces the new contrast set {armchair, chair}, the meaning of the sign “chair” needs to change. In the *Furniture Shopping* scenario, the agreed meaning of that sign can be expressed in a new semiotic triangle  $\langle \text{“chair”}, I', E' \rangle$ , where now the agreed meaning  $I'$  is that of chairs without arms (because when referring to those the agents would use the “armchair” sign); moreover, the set of objects that are reference of the sign is also changed, since  $E'$  is about objects that are chairs but not armchairs.

Specifically, our computational model will assume two agents with possibly different contrast sets, and we assume that each term in a contrast set is a sign  $S_1$  are represented as a semiotic triangle, in which the segregate corresponds to extensional definition  $E_1$  of that triangle. Moreover, disagreements and negotiation of an agreement over meaning will be performed by an argumentation-based communication between two agents, explained in Section 2.

### 1.1. Related work

Ontology alignment has been studied on database schemas, XML schemas, taxonomies, formal languages, entity-relationship models, and dictionaries. Formally, while matching is the process of finding relationships or correspondences between entities of different ontologies, alignment is a set of correspondences between two (or more) ontologies (by analogy with molecular sequence alignment, according to [1]). Thus, the alignment is the output of the matching process.

There are two families of approaches to ontology alignment: (1) syntactic approaches establish matchings among predicates, terms or other structural properties of a formalism, essentially focusing on a notion of similarity; semantic approaches establish logical equivalence correspondences among ontology terms, essentially focusing on a notion of semantic equivalence—in the logical sense of “semantic”. We propose a third approach, a semiotic viewpoint that takes into account both the extensional and intensional definitions of a concept. Moreover, we have an agent-based approach: here each concept mapping is performed inside each individual agent, not by a third party comparing two (external) ontologies. Finally, we do not deal with files specifying a set of concepts (ontology), as is the



**Figure 1.** A contrast set is a set of concepts that partition a domain of examples. To mutually adapt their meaning of concepts, each agent can create a new contrast set (in addition the old one) that allows it to reach an agreement over the meaning of a concept that arises a disagreement in the old contrast set.

common approach, we deal with agents that argue and agree over concepts based on how the concepts are *used* in a particular context. Indeed, the present work expands the agent-based “concept convergence” approach in [3], where argumentation and agreement among was not contextual and focused on a single, isolated concept, not a contrast set.

## 2. Approach

In this section we will present with more details the general ideas introduced in the previous part. Then, we will describe the argumentation protocol which allows the mutual ineligibility between speakers (agents) in different scenarios where the meaning is context dependent.

### 2.1. Concepts and Contrast Set

As we said, a concept  $C_i$  is understood as a semiotic triangle, i.e. composed of a sign  $s_i$ , an intensional definition  $I(C_i)$  and an extensional definition  $E(C_i)$ . We use the notation  $C_i = \langle s_i, I(C_i), E(C_i) \rangle$  to represent a concept  $C_i$  (Fig. 1).  $E(C_i)$  is understood as the set of objects or examples known by the agent as belonging to concept  $C_i$ . The intensional definition  $I(C_i)$  contains a set  $\alpha_1 \dots \alpha_m$  of generalizations such that  $\forall e \in E(C_i), \exists \alpha \in I(C) : \alpha \sqsubseteq e$  and  $\forall \alpha \in I(C), \exists e \in E(C_i) : \alpha \sqsubseteq e$ . We will use the notation  $I(C_i) \sqsubseteq e$  when there is a generalization in the intensional definition that subsumes the example  $e$ , and to say that an example belongs to the concept which sign is  $s_i$  we will also use the notation  $s_i \sqsubseteq e$ .

We introduced the notion of contrast set as a collection of concepts that induces a partition on a domain; we will now define a contrast set in which concepts are represented by the semiotic triangle with our terminology. A contrast set  $K$  consists of a collection concepts  $K = (C_1, \dots, C_n)$ , with a collection of signs  $s(K) = (s_1, \dots, s_m)$ , a collection of intensional definitions  $I(K) = (I(C_1), \dots, I(C_m))$ , and set of examples  $E(K) = E(C_1) \cup \dots \cup E(C_m)$  belonging to those concepts. Since a contrast set determines a partition of the elements in  $E(K)$ , now each

intensional definition  $I(C_i) \in I(K)$  has to comply with the following property:  $\forall e \in E(K) \setminus E(C_i) : I(C_i) \not\sqsubseteq e$  —i.e. the generalizations in  $I(C_i)$  shouldn't subsume an example also subsumed by a generalization from an intensional definition of another concept in the contrast set.

To explore the notion of agreement over the meaning, we use a scenario with two agents that have individual (and possibly different) contrast sets over the same domain. The agents jointly observe new elements in this domain, and categorizing elements in one of the concepts of their individual contrast sets. Disagreement arises when the *signs* of the concepts in which an element is categorized are different. Upon disagreement, the agents engage in an exchange of arguments to adapt their individual contrast sets to one another until the disagreement is solved. This is an iterative process in which both agents build two new contrast sets that are closer:  $K_1 \xrightarrow{\text{adapt}} K'_1 \rightleftharpoons K'_2 \xleftarrow{\text{adapt}} K_2$  (see Fig. 1 and Fig. 2).

## 2.2. Communication Protocol

We assume that our agents already share the language  $\mathcal{L}$  and are able to exchange information through a communication protocol that we will specify in the next section using messages from the following list:

- *Assert*( $s, e$ ): this message asserts that the sending agent considers  $e$  to be an example belonging to the same concept as the sign  $s$  ( $s \sqsubseteq e$ ).
- *Accept*( $s, e$ ): this message asserts that the sending agent agrees on fact that  $e$  is in the concept whose sign is  $s$  ( $s \sqsubseteq e$ ).
- *Refuse*( $s, e$ ): this message asserts that the sending agent disagrees on fact that  $e$  is in the concept whose sign is  $s$  ( $s \not\sqsubseteq e$ ).
- *Ask*( $s, e$ ): this message asks to the other agent which generalization, in the concept whose sign is  $s$ , subsumes  $e$ .
- *Answer*( $s, \beta, e$ ): sends the generalization  $\beta$ , in the concept whose sign is  $s$ , that subsumes  $e$  ( $\beta \sqsubseteq e$ ).

In order to explore the possibilities offered by the use of contrast sets, we implemented three different scenarios that we present in the next part. We will now present the protocol used by two agents to build and organize their contrast sets in order to achieve a mutual agreement. A sketch of the protocol is as follows:

1. The two agents are waiting (*Initial state*)
2. An example  $e_x$  is presented to the agents. Each agent  $A_i$  categorizes the example with a sign  $s_i$  and sends *Assert*( $s_i, e_x$ ) to the other agent.
3. Each agent verifies whether the received sign  $s_j$  is in its contrast set. If the sign is unknown the agent goes to step 5, otherwise they go to step 4.
4. Each agent verifies whether  $s_j \sqsubseteq e_x$  in its individual contrast set:
  - if it is true, the agent has no disagreement over the meaning of  $s_j$  ( $s_i = s_j$ ) and sends the message *Accept*( $s_j, e_x$ ). The agent goes to step 1.
  - if it is not true, the two agents are going to create new concepts in order to reach an agreement over the contextual meaning of the sign used. They go to step 5.

5. There is at least one agent which does not know one of the exchanged signs, e.g.  $s_i$ , then this agent sends a message  $Ask(s_i, e_x)$  to the other agent.
6. The other agent sends back an  $Answer(s_i, \alpha_m, e_x)$  where  $\alpha_m$  is the generalization that subsumes  $e_x$  ( $\alpha_m \sqsubseteq e$ ).
7. The agent that did not know  $s_i$  uses the received generalization  $\alpha_m$  to check if the unknown sign is a synonym or an hyponym of an already-known concept  $I(C_j)$  (more details are given at the end of the scenario):
  - in case of synonymy, the agent creates a new concept for the sign  $s_i$ .
  - in case of hyponymy, it creates two new concepts; one for  $s_i$  (the unknown sign) and one other for  $s_j$  (the sign this agent sent when categorizing  $e_x$ ).
  - otherwise, the agent sends a  $Refuse(s_i, e_x)$ .
8. The agent incorporates those concepts:
  - if no new contrast set has been created for the current social context yet, the agent creates one and put the new concept(s) into it, while including also the rest of the concepts from the first contrast set that are not affected.
  - if a contrast set has already been created,  $C_i$  is removed from it and the new concept(s) is/are added.
9. The agent returns to 3 (although this time they will not disagree at 4).

We will now provide more details about the internal process occurring during the step 7. When an agents receives the message  $Answer(s_i, \alpha_m, e_x)$ , it starts by creating the set of examples  $E(C_i^*)$  that contains all the examples  $e_i^*$  from the extensional definition  $E(K_l)$  of its current contrast set  $K_l$  which verify the property  $\alpha_m \sqsubseteq e_i^*$ . Then,  $\forall C_j \in K_l$ :

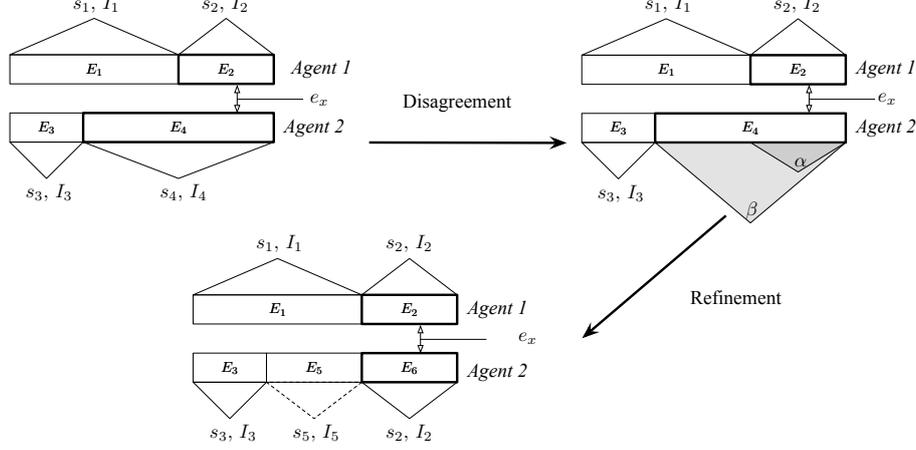
- if  $\exists C_j : E(C_j) = E(C_i^*)$ , then the agent recognizes  $s_i$  as a synonym.
- if  $\exists C_j : E(C_j) \subset E(C_i^*)$ , the agent recognizes  $s_i$  as an hyponym (Fig. 2).

In the case of a synonymy, the new concept created is:  $C_a = \langle s_i, I(C_j), E(C_j) \cup e_x \rangle$ . Since there is a synonymy, there is no need to change the extensional and intensional definitions from the old concept  $C_j$ , except from adding the new example  $e_x$  to the extensional definition of course.

However, in the case of an hyponymy, the agent creates a second new extensional definition  $E(C_j^{**}) = E(C_j) - E(C_i^*)$ . At this point, the agent has created two new concepts, namely  $C_a = \langle s_j, I(C_a), E(C_j^{**}) \rangle$  and  $C_b = \langle s_i, I(C_b) = \alpha_m, E(C_i^*) \cup e_x \rangle$ . After these two concepts are incorporated to the current contrast set we still need to generate the intensional definition of the  $C_a$  concept. Now, in order to create this intensional definition  $I(C_a)$ , we use an argumentation-based inductive learning method [4] that takes set of examples  $E(K_n)$  as positive examples, and the rest of examples in the contrast set as negative examples.

### 3. Scenarios

We present three scenarios to test the agents' ability to reach an agreement over some concept meaning. The examples used during those scenarios are in part of



**Figure 2.** When a new concept is needed, the agent asks the relevant generalization from the other agent's intentional definition of that concept; this generalization (e.g.  $\alpha$ ) leads to a split of the previous extensional definition  $E_4$  in two:  $E_5$  (examples subsumed by  $\alpha$ ) and  $E'_4$  (the rest).

the common sense domain of *seats*. Specifically, examples of seats are divided in three categories (Chairs, Armchairs and Stools), where we are using their typical definitions: (1) a Stool has no back and no arms, (2) a Chair has a back but no arms, and (3) an Armchair has a back and arms. In every scenario, agents  $A_1$  and  $A_2$  start with their own individual contrast set. Given a new example  $e_x$ , they will try to solve their disagreement when it occurs.

### 3.1. Concept Hyponymy

In the first scenario the two agents have initially their contrast sets  $K_1$  and  $K_2$ , shown in Table 1. The first example  $e_1$  presented to both agents is an Armchair. The two agents first send  $Assert(chair, e_1)$  in the case of  $A_1$  and  $Assert(armchair, e_1)$  in the case of  $A_2$ . They both discover a disagreement. The sign  $armchair \notin S(K_1)$  so  $A_1$  sends  $Ask(armchair, e_1)$  to  $A_2$ .  $A_2$  responds with  $Answer(armchair, \beta_2)$  since  $\beta_2 \sqsubset e_1$ . Then,  $A_1$  creates the subset  $E(C_6) = \{e_i \in E(C_2) | \beta_2 \sqsubseteq e_i\}$ . Since  $E(C_6) \neq E(C_2)$ ,  $A_1$  creates the subset  $E(C_5) = E(C_2) - E(C_6)$ . No contrast set has been created yet, so  $A_1$  creates a new contrast set  $K'_1$ . The new concepts  $C_5 = \langle chair, I(C_5), E(C_5) \rangle$  and  $C_6 = \langle armchair, \beta_2, E(C_6) \cup e_1 \rangle$  are added to  $K'_1$  with the concept  $C_1$ . Then,  $A_1$  performs an induction on the new  $E(K'_1)$  for the sign  $chair$  that results to the generalization  $\alpha_3$  which is added to  $I(C_5)$ . Finally,  $A_1$  sends an  $Accept(armchair)$ .

The second example presented,  $e_2$ , is a Chair. The agents send to each other  $Assert(chair, e_2)$ . Since both agents agree on the use of *chair* as a sign to describe a Chair, they just send to each other two messages  $Accept(chair, e_2)$ .

The last example  $e_3$  presented to the agents is a Stool. As with  $e_1$ , they both notice the disagreement over *stool* and *chair*, but this time  $stool \notin K_2$ . It leads  $A_2$  to send  $Ask(stool, e_3)$  to  $A_1$ . Since  $\alpha_1 \sqsubset e_3$ ,  $A_1$  sends back  $Answer(stool, \alpha_1)$ . Now it is  $A_2$ 's turn to create a subset  $E(C_7) = \{e_i \in E(C_3) | \alpha_1 \sqsubseteq e_i\}$ ,

**Table 1.** Initial contrast sets of agents  $A_1$  and  $A_2$ 

C. set	<b>Agent 1 contrast set <math>K_1</math></b>	
Concept	$C_1$	$C_2$
Sign	<i>stool</i>	<i>chair</i>
$I(C)$	$\alpha_1: no.arm, no.back$	$\alpha_2: with.back$
C. set	<b>Agent 2 contrast set <math>K_2</math></b>	
Concept	$C_3$	$C_4$
Sign	<i>chair</i>	<i>armchair</i>
$I(C)$	$\beta_1: no.arm$	$\beta_2: with.arm, with.back$

**Table 2.** Final contrast sets of  $A_1$  and  $A_2$ 

C. set	<b>Agent 1 contrast set <math>K'_1</math></b>		
Concept	$C_1$	$C_5$	$C_6$
Sign	<i>stool</i>	<i>chair</i>	<i>armchair</i>
$I(C)$	$\alpha_1: no.arm, no.back$	$\alpha_3: no.arm, with.back$	$\beta_2: with.arm, with.back$
C. set	<b>Agent 2 contrast set <math>K'_2</math></b>		
Concept	$C_7$	$C_8$	$C_4$
Sign	<i>stool</i>	<i>chair</i>	<i>armchair</i>
$I(C)$	$\alpha_1: no.arm, no.back$	$\beta_4: no.arm, with.back$	$\beta_2: with.arm, with.back$

and since  $E(C_7) \neq E(C_3)$ ,  $A_2$  creates the subset  $E(C_8) = E(C_3) - E(C_7)$ . No new contrast set has been created by  $A_2$ , so it creates  $K'_2$ . The new concepts  $C_7 = \langle stool, \alpha_1, E(C_7) \cup e_3 \rangle$  and  $C_8 = \langle chair, I(C_8), E(C_8) \rangle$  are added to  $K'_2$  with the concept  $C_4$ .  $A_2$  performs an induction on the new  $E(K'_2)$  for the sign *chair*. The resulting generalization  $\beta_4$  is added to  $I(C_8)$ . Finally,  $A_2$  sends an  $Accept(stool, e_3)$  to  $A_1$ . The contrast sets are now as shown in Table 2. We can now see that  $K'_1$  and  $K'_2$  are mutually intelligible.

### 3.2. Concept Synonymy

In the second scenario the two agents have initially their contrast sets  $K_1$  and  $K_2$  are as shown in Table 3. The only example  $e_1$  presented to both agents is an Armchair.  $A_1$  sends  $Assert(armchair, e_1)$  to  $A_2$  and  $A_2$  sends  $Assert(recliner, e_1)$  to  $A_1$ . It leads to a disagreement from both of  $A_1$  and  $A_2$ . Since *armchair*  $\notin K_2$  and *recliner*  $\notin A_1$  neither, both agents can send an *Ask* message. Let's say that  $A_1$  receives the *Ask* message first;  $A_1$  will respond with  $Answer(armchair,$

**Table 3.**  $A_1$  and  $A_2$  contrast sets

C. set	<b>Agent 1 contrast set <math>K_1</math></b>		
Concept	$C_1$	$C_2$	$C_3$
Sign	<i>stool</i>	<i>chair</i>	<i>armchair</i>
$I(C)$	$\alpha_1: no.arm, no.back$	$\alpha_2: no.arm, with.back$	$\alpha_3: with.arm, with.back$
C. set	<b>Agent 2 contrast set <math>K_2</math></b>		
Concept	$C_4$	$C_5$	$C_6$
Sign	<i>stool</i>	<i>chair</i>	<i>recliner</i>
$I(C)$	$\beta_1: no.arm, no.back$	$\beta_2: no.arm, with.back$	$\beta_3: with.arm, with.back$

$\alpha_3$ ), where  $\alpha_3$  is the generalization that was used by  $A_1$  to categorize  $e_1$ .  $A_2$  creates a new set of examples  $E(C_7) = \{e_i : e_i \in E(C_6) | \alpha_3 \sqsubseteq e_i\}$ . No contrast set has been created before so  $A_2$  creates  $K'_2$ . Since  $E(C_7) = E(C_6)$ , a new concept  $C_7 = \langle \text{armchair}, I(C_6), E(C_6) \cup e_1 \rangle$  is created and added to  $K'_2$  along with  $C_4$  and  $C_5$ . *Accept*(*armchair*,  $e_1$ ) is sent to  $A_1$  by  $A_2$ . We notice that if  $A_1$  had been faster than  $A_2$  to send its *Ask* message, it is *recliner* that would have been used to designate an Armchair by both agents. This would not have affect the reach of mutual intelligibility.

### 3.3. Concept Teaching

This time  $K_1$  is still as it was in Table 3 but  $K_2$  is modified as shown in Table 4. The first example  $e_1$  presented to the agents is a Stool.  $A_1$  sends *Assert*(*stool*,  $e_1$ ) to  $A_2$  and  $A_2$  *Assert*(*seat*,  $e_1$ ) to  $A_1$ . Since *seat*  $\notin S(K_1)$  and *stool*  $\notin S(K_2)$ , each agent can send an *Ask* message to the other. Let's say that  $A_1$  is the fastest to send its *Ask*(*seat* message,  $e_1$ ),  $A_2$  sends *Answer*(*seat*,  $e_1$ ).*any*  $\sqsubset \alpha_1, \alpha_2$  and  $\alpha_3$ :  $A_1$  sends *Refuse*(*seat*,  $e_1$ ) to  $A_2$ . Now  $A_2$  sends *Ask*(*stool*,  $e_1$ ) to  $A_1$ .  $A_1$  sends back *Answer*(*stool*,  $\alpha_1$ ). Now  $A_2$  creates the subset  $E(C_5) = \{e_i : e_i \in E(C_4) | \alpha_1 \sqsubseteq e_i\}$ , and since  $E(C_5) \neq E(C_4)$ ,  $A_2$  also creates the subset  $E(C_6) = E(C_4) \setminus E(C_5)$ . No contrast set has been created yet so  $A_2$  creates  $K'_2$ . The new concepts  $C_5 = \langle \text{stool}, \alpha_1, E(C_5) \cup e_1 \rangle$  and  $C_6 = \langle \text{seat}, I(C_6), E(C_6) \rangle$  are added to  $K'_2$ . New generalizations for *seat*,  $\beta_3 = \text{with.back}$  and  $\beta_4 = \text{with.arm}$ , are learned by induction from  $E(K'_2)$  and added to  $I(C_6)$ .

The second example presented  $e_2$  is a Chair.  $A_1$  sends *Assert*(*chair*,  $e_2$ ) to  $A_2$  and  $A_2$  *Assert*(*seat*,  $e_2$ ) to  $A_1$ . Again, *seat*  $\notin S(K_1)$  and *chair*  $\notin S(K'_2)$  so each agent can send an *Ask* message to the other. Let's say that this time  $A_2$  is faster and sends *Ask*(*chair*,  $e_2$ ) to  $A_1$ .  $A_1$  sends back *Answer*(*chair*,  $\alpha_2$ ) since  $\alpha_2 \sqsubset e_2$ .  $A_2$  creates a new set  $E(C_7) = \{\forall e_i : e_i \in E(C_6) | \alpha_2 \sqsubseteq e_i\}$ , and since  $E(C_7) \neq E(C_6)$ ,  $A_2$  also creates the subset  $E(C_8) = E(C_6) \setminus E(C_7)$ . The new concepts  $C_7 = \langle \text{chair}, \alpha_2, E(C_7) \cup e_2 \rangle$  and  $C_8 = \langle \text{seat}, I(C_8), E(C_8) \rangle$  are added to  $K'_2$ . The concept  $C_6$  is removed from  $K'_2$ . A generalization for *seat*,  $\beta_6$ , is learned by induction from  $E(K'_2)$  and put into  $I(C_8)$ .  $A_2$  sends *Accept*(*chair*,  $e_2$ ) to  $A_1$ .

The last example presented  $e_3$  is an Armchair.  $A_1$  sends *Asset*(*armchair*,  $e_3$ ) to  $A_2$ . Meanwhile  $A_2$  sends *Assert*(*seat*,  $e_3$ ) to  $A_1$ . Since *seat*  $\notin S(K_1)$  and *armchair*  $\notin S(K'_2)$ , both agents can send an *Ask* and let's say that this time again  $A_2$  is quicker and sends *Ask*(*armchair*,  $e_3$ ) to  $A_2$ . Since  $\alpha_3 \sqsubset e_3$ ,  $A_1$  sends

**Table 4.**  $A_2$ 's contrast sets before teaching

C. set	<b>Agent 2 contrast set <math>K_2</math></b>
Concept	$C_4$
Sign	<i>seat</i>
$I(C)$	$\beta_1 : \text{any}$

**Table 5.**  $A_1$  and  $A_2$  Contrast sets after the last concept learning

C. set	<b>Agent 2 contrast set <math>K'_2</math></b>		
Concept	$C_5$	$C_7$	$C_9$
Sign	<i>stool</i>	<i>chair</i>	<i>armchair</i>
$I(C)$	$\beta_2 : \text{no.arm, no.back}$	$\alpha_2 : \text{no.arm, with.back}$	$\beta_6 : \text{with.arm, with.back}$

back  $Answer(\textit{armchair}, \alpha_3)$ . After receiving the answer,  $A_2$  creates a new set of examples  $E(C_9) = \{\forall e_i : e_i \in E(C_8) | \alpha_3 \sqsubseteq e_i\}$ . Since  $E(C_9) = E(C_8)$ , a new concept  $C_9 = \langle \textit{armchair}, I(C_8), E(C_8) \cup e_3 \rangle$  is created and added to  $K'_2$  while  $C_8$  is removed. An  $Accept(\textit{armchair}, e_3)$  is sent to  $A_1$ . Table 5 shows the new  $K'_2$ .

## Discussion and Future Work

We have put together for the first time in a computational model the notions of semiotic triangle and contrast sets, coming from very different fields of study, namely semiotics and ethnographic studies. We have shown how these notions can be given a computational model to represent concepts and the adaptation of concept meaning in particular contexts. We have also shown that message passing communication among agents can be understood as arguments exchanged between the agents that trigger the necessary changes for adaptation. However, we made certain assumptions to simplify the types of disagreement that may arise. For this reason, the communication protocol only considers a limited number of disagreements can arise, as shown in the “simple” scenarios presented. Nevertheless, the experiments show that a range of common scenarios in contextual meaning adaptation are within the scope of the current approach (concept refinement, synonymy detection).

There are three lines of future research that extend beyond the current assumptions. The first one is that the two contrast sets may have overlapping extensional definitions of concepts, a situation we assumed did not happen in our simple scenarios. This would allow a more complex argumentation model, where counter-arguments and counter-examples of one agent can attack the arguments of the other agent. A second line of research is having several levels of contrast set with different granularities (i.e. a taxonomical terminology). The third line of research is a recursive approach, in which specific predicates in  $\mathcal{L}$  may also be unknown or not agreed-upon, e.g. they disagree on what constitutes of not an *arm* of seat, and then agents may initiate a new a dialogue to achieve an agreement over meaning. After this agreement is reached, the agents can return to the higher level dialogue.

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